

# SOLUTION

Write your solutions in steps.

1. (3 points) Evaluate  $\int_2^5 \sqrt{x-1} dx$

2. (3 points) Compute  $\int x \sin x dx$

3. (4 points)  $f(x)$  is a function such that  $f'(x) = x^2 e^x$  and  $f(0) = 3$ . Find  $f(1)$ .

$$\begin{aligned}
 (1). \int_2^5 \sqrt{x-1} dx & \quad (u = x-1, \\
 & \quad du = dx). \\
 & = \int_1^4 \sqrt{u} du \\
 & = \frac{2}{3} u^{\frac{3}{2}} \Big|_1^4 \\
 & = \frac{2}{3} \left( 4^{\frac{3}{2}} - 1^{\frac{3}{2}} \right) \\
 & = \frac{14}{3}
 \end{aligned}$$

$$\begin{aligned}
 (2). \int x \sin x dx & = - \int x d \cos x \\
 & = -x \cos x + \int \cos x dx \\
 & = -x \cos x + \sin x + C
 \end{aligned}$$

$$\begin{aligned}
 (3). f(1) - f(0) & = \int_0^1 f'(x) dx = \int_0^1 x^2 e^x dx \\
 & = \int_0^1 x^2 de^x \\
 & = x^2 e^x \Big|_0^1 - \int_0^1 e^x dx^2 \\
 & = e - 2 \int_0^1 x e^x dx \\
 & = e - 2 \int_0^1 x de^x \\
 & = e - 2 \left( x e^x \Big|_0^1 - \int_0^1 e^x dx \right) \\
 & = e - 2 \left( e - e^x \Big|_0^1 \right) \\
 & = e - 2
 \end{aligned}$$

so  $f(1) = f(0) + (e-2) = e+1$